

Crystal structure of a silica- and alkali-rich trioctahedral mica

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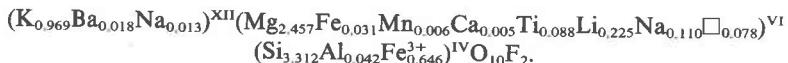
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Abstract

The crystal structure of a trioctahedral mica of unusual composition from melilite-bearing eruptive rocks has been determined ($R = 3.0\%$). This mica, which has excess silica ($\text{Si} > 3$) and alkalis ($\sum \text{Na} + \text{K} > 1$), is the first known layer silicate with octahedral sodium. In spite of the complexity of the octahedral layer, which includes Mg, Fe, Li, Ca, Mn, Na, Ti, and vacancies, there is no evidence for cation ordering between the two distinct octahedral sites. Both sites have the same mean M–O distance (2.077 Å) and the same electron density. The structural formula of the mica, based on chemical analysis and the structure refinement, is:



Introduction

Velde (1979) described a suite of trioctahedral micas of various compositions from melilite-bearing eruptive rocks. Of special interest is a group of silica-rich micas, characterized by high alkalis and ferric iron and low aluminum, in addition to significant amounts of Li, Ba, and Ti. These micas are unusual because $\sum(\text{K} + \text{Na} + \text{Ba}) \gg 1.0$, $\text{Si} \gg 3.0$, and $\sum(\text{Si} + \text{Al}) \ll 4.0$. Substantial deviations from the ideal biotite, $(\text{K},\text{Na})(\text{Mg},\text{Fe})_3\text{AlSi}_3\text{O}_{10}(\text{OH})_2$, therefore obtain. The principal objective of this study is to document the site distributions of cations in this mica.

Experimental

Euhedral single crystals of a silica-rich mica (sample Y253, Gragnani, 1972) from the type copaelite, at Cupaello, Italy, were selected for X-ray investigation. These crystals are unzoned and display a slight reverse pleochroism, characteristic of micas with tetrahedral Fe^{3+} (Hazen and Wones, 1972).

The composition of the crystals was determined by ion and electron microprobe analysis (Table 1). Fluorine was detected in significant amounts (>3 wt.%) by both ion and electron microprobe, but exact

quantitative determination could not be made. No OH^- was detected by infrared analysis and the mica thus has $\text{F}/(\text{F} + \text{OH}) \approx 1$. It is not known if there is a significant oxy-biotite component. Ion microprobe analysis indicated 0.75 ± 0.25 wt.% Li_2O (tourmaline standard), and boron in only trace amounts.

X-ray diffraction photographs of a crystal plate $140 \times 130 \times 50 \mu\text{m}$ revealed sharp diffraction maxima with none of the smearing or streaking of spots characteristic of deformed crystals or disordered stacking arrangements. Unit-cell parameters of this silica-rich mica (Table 2) are typical for a one-layer trioctahedral mica with potassium in the interlayer position (Hazen and Wones, 1972).

All X-ray reflections in one octant of reciprocal space ($\sin \theta/\lambda < 0.9$) were collected on an automated four-circle diffractometer with Nb-filtered $\text{MoK}\alpha$ radiation (Finger *et al.*, 1973). All reflections were corrected for specimen absorption ($\mu_i = 21.0 \text{ cm}^{-1}$) as well as Lorentz and polarization effects. A total of 625 nonequivalent data were observed ($I > 2\sigma_i$). Trial refinements in space group $C2$, in which adjacent tetrahedra are symmetrically independent, and $C2/m$, in which all tetrahedra are equivalent, yielded similar results. The $C2/m$ refinement yielded the residual of

Table 1. Composition and calculated structural formula of silica-rich trioctahedral mica

Wt. %	No. Atoms	Per Site			Value
		No. Atoms	No. Charges	No. Electrons*	
SiO ₂	44.43	3.312			
Al ₂ O ₃	0.47	0.042			
B ₂ O ₃	trace				
Fe ₂ O ₃	11.38	0.646			
FeO†	0.49	0.031			
MgO	22.11	2.457			
MnO	0.09	0.006			
CaO	0.07	0.005			
TiO ₂	1.57	0.088			
Li ₂ O‡	0.75	0.225			
Na ₂ O	0.84	0.110			
		0.013			
BaO	0.62	0.018			
K ₂ O	10.18	0.969			
F§	4.5	2.000			
H ₂ O	(<0.1)				
Totals	97.50	7.922	+22.01		

*Number of electrons per site = Σ (number of atoms per site \times atomic number).

†Octahedral Fe²⁺/Fe³⁺ is unknown.

‡Based on ion probe analysis with tourmaline standard. Value cited is ± 0.25 weight percent.

§Fluorine present in significant amounts (>3%), based on ion and electron microprobe analysis. Calculations are based on end member fluoro-mica.

||Based on infrared spectra analysis by B. Velde.

Table 2. Unit-cell dimensions

Unit-Cell Parameter*	Value
a (Å)	5.3290(9)†
b (Å)	9.2300(15)
c (Å)	10.2191(11)
α (°)	90.00(1)
β (°)	99.98(1)
γ (°)	90.01(1)
V (Å ³)	495.0(1)

*Refinement of unit-cell parameters from diffractometer data was unconstrained (i.e. triclinic).

†Parenthesized figures represent esd's.

Table 3. Refinement conditions

Parameter	Value
Weighted R (%)*	3.0
R (%)†	3.0
No. of observations	625
Extinction parameter	0.6(+1.2) $\times 10^{-5}$
Weighted R = $[\sum w(F_O - F_C)^2 / \sum w F_O^2]^{1/2}$.	
†R = $\sum F_O - F_C / \sum F_O $.	

greatest significance, however, and the centrosymmetric space group, as observed in previous refinements of one-layer biotites, was thus selected. All observed reflections were included in the refinement of atomic positions, anisotropic thermal parameters, unconstrained occupancy factors for all metal sites and the fluorine site, and an isotropic extinction parameter. Conditions of refinement are recorded in Table 3, refined positional and thermal parameters in Table 4, and observed and calculated structure factors in Table 5. Least-squares weights were derived from

standard deviations based on counting statistics to which an amount equivalent to 2% of F^2 has been added.

Results and discussion

Interatomic distances and angles (Table 6) and the orientations and magnitudes of thermal vibration ellipsoids (Table 7) are similar to those of previously reported trioctahedral micas in the phlogopite-annite series (Hazen and Burnham, 1973; Bohlen *et al.*, 1980). The 5.7° tetrahedral rotation angle, which is

Table 4. Refined atomic coordinates, anisotropic temperature factors, equivalent isotropic temperature factors, and number of electrons per metal site in silica-rich trioctahedral mica

Atom	x	y	z	β_{11}	β_{22}	β_{33}	β_{12}	β_{13}	β_{23}	B	No. of Electrons
T	0.5749(1)	0.1667(1)	0.2255(1)	0.0082(2)	0.0022(1)	0.0023(1)	-0.0000(1)	0.0007(1)	-0.0001(1)	0.87(1)	15.0(2)
M1	0	1/2	1/2	0.0063(5)	0.0012(2)	0.0026(2)	0	0.0008(2)	0	0.71(4)	11.7(2)
M2	0	0.8337(1)	1/2	0.0061(4)	0.0019(1)	0.0025(1)	0	0.0007(2)	0	0.78(3)	11.7(2)
K	0	0	0	0.0227(5)	0.0068(2)	0.0057(1)	0	0.0016(2)	0	2.40(3)	19.3(2)
O1	0.8198(3)	0.2355(2)	0.1672(2)	0.0236(8)	0.0097(3)	0.0042(2)	-0.0036(4)	0.0012(3)	-0.0003(2)	2.55(4)	
O2	0.5264(6)	0	0.1669(2)	0.0347(13)	0.0066(3)	0.0041(3)	0	0.0011(5)	0	2.61(6)	
O3	0.6298(3)	0.1670(2)	0.3901(1)	0.0096(5)	0.0026(2)	0.0027(1)	-0.0001(2)	0.0006(2)	0.0000(1)	1.03(3)	
F	0.1336(4)	0	0.3992(2)	0.0113(8)	0.0035(2)	0.0027(2)	0	0.0007(3)	0	1.19(5)	8.3(2)

*Number of electrons is refined for each cation site based on electron density. No constraints are used.

Table 5. (continued)

L	OBS	CALC	L	OBS	CALC	L	OBS	CALC	L	OBS	CALC	L	OBS	CALC	L	OBS	CALC
4	0	L	-2	2	L	1	3	L	-5	5	L	2	6	L	4	8	L
1	629	631	1	404	397	0	744	720	2	89	94	0	986	982	0	147	155
2	154	147	2	422	426	1	376	346	3	130	138	1	831	827	1	181	201
3	228	222	3	241	248	2	417	404	4	255	257	2	123	129	3	102	116
4	834	855	4	186*	238	3	690	674	6	101	100	3	363	378	5	247	237
5	648	653	5	176	177	4	458	449	8	178	196	4	1035	1042	6	152	158
6	234	237	6	328	301	5	1034	1031	9	130	142	5	76	72	1	244	247
8	341	344	7	614	622	6	1199	1209	10	77	74	6	144	156	-5	9	L
9	103	117	8	336	330	7	268	276				8	361	371	2	71	29
10	139	134	9	250	255	8	171	173	-3	5	L	10	72	17	3	275	276
			10	190	195	9	645	639				11	302	301	4	129	140
6	0	L	11	139	131	10	100	92	1	225	236	4	268	269	0	12	L
			12	290	295	11	260	252	2	110	115	5	131	137	0	720	724
1	168	169	13	152	139	13	416	405	3	548	533	1	340	331	-3	9	L
2	345	352	14	92	100				4	310	308	2	273	264	1	163	158
3	206	196				3	3	L	5	127	126	3	169	160	3	236	223
4	101	94	0	2	L				6	165	160	1	801	803	4	279	290
5	323	330				0	481	478	7	125	143	4	484	488	2	206	199
6	398	390	0	418	435	1	54	62	8	309	314	5	625	625	5	244	235
			1	93	95	2	275	271	9	76	63	6	201	186	5	363	364
-7	1	L	2	895	897	3	677	656	10	74	57	7	143	130	6	200	199
			3	639	638	4	467	467	12	93	111	8	354	352	7	111	98
2	93	94	4	55	9	5	107	111				8	333	334	0	359	370
4	157	165	5	97	95	6	597	575	-1	5	L	6	6	L	1	376	378
5	157	160	6	194	194	7	597	593				9	400	396	2	94	90
			7	411	409	8	74	93	1	166	163	0	81	60	3	94	102
-5	1	L	8	70	48	9	401	389	2	372	363	1	228	218	-1	9	L
			10	150	140	10	461	467	3	533	522	2	281	275	1	527	530
1	83	78	11	200	198	11	92	65	4	118	109	3	231	228	2	648	647
2	120	110	12	99	105				5	69	53				3	210	211
3	185	182	13	110	113	5	3	L	6	96	84	-5	7	L	4	93	88
4	346	350							7	311	306				5	799	803
5	85	75	2	2	L	0	622	627	8	104	101	1	90	100	6	189	192
6	119	126				1	212	207	9	104	99	2	100	109	7	266	265
8	223	222	0	407	400	2	95	94	10	75	75	3	126	149	9	377	384
9	167	182	1	420	424	3	784	786	11	188	188	4	281	277	10	76	97
			2	83	86	4	172	184	12	158	148	5	90	62			
-3	1	L	3	311	306	5	248	257	13	79	65	6	117	121	1	9	L
			5	434	443	7	370	374				8	154	152			
1	255	256	6	616	620	8	122	97	1	5	L			0	371	372	
2	136	136	7	106	112							-3	7	L	1	69	23
3	622	636	8	318	315	7	3	L	0	200	198				2	341	339
4	384	394	10	201	208				1	360	350	1	143	148	3	269	266
5	115	113	11	292	291	0	269	262	2	663	658	3	317	310	4	159	164
6	121	131				1	134	129	3	202	200	4	203	198	5	488	495
7	182	177							4	173	173	7	160	156	6	629	630
8	352	362				-6	4	L	5	62	54	8	213	217	7	190	189
10	68	67							6	299	297	10	88	74	8	139	131
11	87	82				2	137	147	7	294	305	11	91	75	9	342	353
12	150	150				4	194	199	10	100	114						
			5	157	155	11	163	160				-1	7	L			
			8	97	86							2	447	444			
			9	125	125							3	459	461			
												5	188	193			
												7	309	312			
												8	172	167			

related to the relative sizes of octahedral and tetrahedral layers, is also typical of other trioctahedral micas.

It is important to resolve the distribution of cations among the four different metal sites (the interlayer site, the tetrahedral site, and two symmetrically distinct octahedral sites). The structure refinement with unconstrained metal occupancy factors, combined with chemical analysis (Table 1), are sufficient to derive a reasonable, if not unique, structural formula

for this unusual mica. A crystal-chemical constraint common to all micas is that there must be exactly four tetrahedral cations per 11 oxygens. Of the cations present (Table 1), only Si, Al, and Fe³⁺ commonly enter tetrahedral coordination in micas. Magnesium has been observed in four coordination in iron-free synthetic mica (Tateyama, 1974), but tetrahedral magnesium has not been reported from natural micas, nor has it been observed in any mica with $\Sigma(\text{Si} + \text{Al} + \text{Fe}^{3+}) \geq 4$. Furthermore, the refined elec-

Table 6. Interatomic distances and bond angles

Bond	Distance (Å)	Atoms	Angle (°)	Bond	Distance (Å)	Atoms	Angle (°)
<u>Tetrahedron</u>							
T-01	1.653(2)*	01-T-01	108.16(7)	M1-03[4]	2.093(1)	03-M1-03[2]	94.80(8)
T-01	1.654(2)	01-T-02	108.08(13)	M1-F[2]	2.044(2)	03-M1-03[2]	85.20(8)
T-02	1.655(1)	01-T-02	110.74(8)	Mean M1-O	2.077	03-M1-F[4]	96.04(5)
T-03	1.657(2)	01-T-03	108.06(13)			03-M1-F[4]	83.96(5)
Mean T-O	1.655	01-T-03	110.75(9)	03-03[2]	2.834(3)	Mean O-M-O	90.00
		02-T-03	110.95(10)	03-03[2]	3.074(3)	(adjacent)	
01-01	2.678(1)		109.46	03-F[4]	2.767(2)		
01-02	2.677(3)			03-F[4]	3.075(2)	03-M1-03	180.00
01-02	2.677(3)			Mean O-O	2.932	F-M1-F	180.00
01-03	2.723(2)			(adjacent)		(opposite)	
01-03	2.725(2)			<u>M1 Octahedron</u>			
02-03	2.729(3)			M2-03[2]	2.092(2)	03-M2-03	85.27(9)
Mean O-O	2.701			M2-03[2]	2.094(1)	03-M2-03[2]	85.26(6)
T-T[2]†	3.076(1)			M2-F[2]	2.044(2)	03-M2-03[2]	94.49(6)
T-T	3.078(1)			Mean M2-O	2.077	03-M2-F[2]	83.93(7)
Mean T-T	3.077					03-M2-F[2]	96.33(7)
<u>Interlayer Site</u>							
K-01[4]	3.022(2)			03-03[2]	2.835(3)	03-M2-F[2]	96.06(6)
K-02[2]	3.020(3)			03-03	3.082(3)	F-M2-F	82.66(9)
Mean K-O (inner)	3.021			03-03[2]	3.074(3)	Mean O-M2-O	90.00
K-01[4]	3.282(2)			03-F[2]	2.767(2)	(adjacent)	
K-02[2]	3.282(3)			03-F[2]	3.074(3)		
Mean K-O (outer)	3.282			03-F[2]	3.084(3)	03-M2-03	179.66(9)
Δ(K-O)	0.261			F-F	2.707(4)	03-M2-F	177.83(7)
				Mean O-O	2.955	Mean O-M2-O	178.75
				(adjacent)		(opposite)	

*Parenthesized figures represent esd's.

†Bracketed figures represent multiplicity.

Table 7. Magnitudes and orientations of thermal ellipsoids

Atom	Axis	rms Displace- ment (Å)	Angle with respect to:		
			a (°)	b (°)	c (°)
T	r_1	0.097(1)*	89(6)	6(5)	84(4)
	r_2	0.107(1)	158(12)	87(6)	102(12)
	r_3	0.110(1)	112(12)	95(4)	14(11)
M1	r_1	0.071(5)	90	0	90
	r_2	0.093(4)	178(7)	90	82(7)
	r_3	0.115(4)	92(7)	90	8(7)
M2	r_1	0.091(3)	90	0	90
	r_2	0.092(3)	175(5)	90	85(5)
	r_3	0.114(3)	95(5)	90	5(5)
K	r_1	0.171(2)	73(9)	90	27(9)
	r_2	0.172(2)	90	0	90
	r_3	0.180(2)	17(9)	90	117(9)
O1	r_1	0.145(3)	83(5)	83(4)	17(6)
	r_2	0.168(3)	147(3)	121(3)	72(6)
	r_3	0.218(3)	58(3)	148(3)	93(2)
O2	r_1	0.146(5)	89(2)	90	11(2)
	r_2	0.168(4)	90	0	90
	r_3	0.223(4)	1(2)	90	101(2)
O3	r_1	0.107(3)	83(17)	9(21)	86(14)
	r_2	0.110(4)	139(17)	81(21)	120(17)
	r_3	0.118(3)	50(16)	90(10)	150(17)
F	r_1	0.118(4)	72(17)	90	27(17)
	r_2	0.123(4)	90	0	90
	r_3	0.128(4)	18(17)	90	117(17)

*Parenthesized figures represent esd's.

tron density of the T site is significantly greater than that of Si, Al or Mg. It is assumed, therefore, that all silicon plus aluminum, as well as 0.646 atoms of Fe^{3+} , occupy this site. The total number of electrons on the tetrahedral site (15.1e^- based on refined electron density) and the mean T-O bond distance (1.655\AA) from the structure refinement, conform well with this assumed tetrahedral site occupancy.

A second crystal-chemical constraint of all micas is that there can be no more than 1.0 interlayer cation per 11 oxygens. In this mica the sum of (K + Na + Ba) is 1.11, indicating that a significant fraction of these cations are not in the interlayer position. All K + Ba, as well as 0.013 atoms of Na, are assigned to a fully-occupied interlayer site. The total number of electrons (19.3e^-) and the mean inner and outer K-O distances (3.021 and 3.282\AA , respectively) from the structure refinement are consistent with this assignment.

All remaining cations must occupy the two octahedral sites. This necessary conclusion leads to one of the most complex site compositions in any known silicate. The resulting average octahedral layer compo-

sition, based on three octahedral cations per 11 oxygens, is:



The remarkable M1 and M2 sites thus have cations of valence 4+, 2+, and 1+, as well as vacancies, with cation radii ranging from 0.61 to 1.02 Å (Shannon, 1976). The total refined number of electrons on the two sites, M1 and M2, are both 11.7 e⁻, and the mean M1-O and M2-O distances are both 2.077 Å. Although the complexity of the octahedral site chemistry precludes a unique solution to M1-M2 cation distribution, there is no evidence for cation ordering, consistent with previous refinements of both igneous (Hazen and Burnham, 1973) and metamorphic (Bohlen *et al.*, 1980) biotites, as well as synthetic BaLiMg₂AlSi₃O₁₀F₂ (McCauley and Newnham, 1973).

The resulting mica, though complex, may be represented as composed primarily (65%) of the ferriphlogopite end member, KMg₃Fe³⁺Si₄O₁₀F₂. Additional components include 23% of the magnesium lithium mica taeniolite, K(LiMg₂)Si₄O₁₀F₂, plus minor amounts of the phlogopite-annite series and a Ti-mica. Note that the calculated number of titanium atoms approximately equals the number of octahedral vacancies, as observed in many other biotites (Hazen and Burnham, 1973). The only previously unknown component of this mica is approximately 4% of an end member with Na in the octahedral layer.

Analytical uncertainties for fluorine, lithium, and octahedral Fe²⁺/Fe³⁺ result in small but significant uncertainties in the structural formula. For example, 10% oxy-biotite substituting for fluoro-biotite could increase the total number of cations from 7.92 to the ideal value of 8.00. Refined electron density of the fluorine site (8.3 e⁻) is smaller than the 9.0 e⁻ value expected for a pure fluoro-mica. This electron deficiency may imply the presence of an oxy-biotite component or undetected (OH)⁻. Uncertainties in lithium content may also affect the structural formula. If total lithium is 0.50 instead of 0.75 wt.%, then the num-

ber of octahedral cations will decrease from 2.92 to 2.85.

This unusual mica serves a special role in the crystallization history of the melilite-bearing eruptive rocks in which it is found. It appears to concentrate alkali metals, including potassium, sodium, and lithium, in an environment that is deficient in aluminum and thus underscores the adaptability of the mica structure to a wide range of compositional limits.

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